# AUTOMATIC CONTINGENCY SELECTION

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## Abstract

- Paper by G.C. Ejebe and B.F. Wollenberg submitted to the IEEE Transactions on Power Apparatus and Systems in 1979.
- A fast technique for the automatic ranking and selection of contingency cases for a power system contingency analysis study.
- Contingencies are ranked according to their expected severity as reflected in voltage level degradation and circuit overloads.
- An adaptive contingency processor can be set up by performing sequential contingency tests starting with the most severe and stopping when the severity drops below a certain threshold.
- Numerical examples on several test cases are provided.

## **Presentation Summary**

- Introduction to Methodology
- System Performance Indices
  - System Performance Index for Voltage Analysis
  - System Performance Index for Power Flow Analysis
  - Other Contingency Ranking Methods
- Creating Ordered Contingency Lists
- Numerical Examples
- Stopping Criteria for the Adaptive Contingency Processor
- Conclusions

## INTRODUCTION TO METHODOLOGY

## Traditional Approach

- Simulate outages to determine impact on bus voltages and power flow using fast computational techniques
- Time-consuming and costly
- Contingencies often selected based on planner's experience
- In real time, contingency testing is up to operator
  - System is constantly changing so impact is different than what may have been determined to be "worst case" by planners

## **Proposed Solution**

- Purpose is to be able to rank contingencies by severity
- Method uses Tellegen's theorem to order the outages
- Non-linear AC load flow equations are used to evaluate contingencies based on voltage quality
- Simplified DC load flow model is used to evaluate contingencies based on power flow
- Method DOES NOT indicates if the contingency will cause problems, just ranks them in order of severity
- Result is a list of contingencies from "worst" to "best"
  - You can then run detailed analysis starting at top of list until you reach a case that does not cause system issues

#### Adaptive Contingency Processor



## SYSTEM PERFORMANCE INDICES

## Background

- Traditional approach is to model outage, perform load flow calculations, and check for:
  - I. Bus voltages outside of normal limits
  - 2. Branch power flows outside of normal operating limits
- Proposed method uses these two sets of limits to develop system performance indices reflecting the contingency severity
  - Limits are treated as soft constraints to rank contingencies

## I. Index for Voltage Analysis

$$PI_V = \sum_{i=1}^{NB} \frac{W_{V_i}}{2n} \left(\frac{|V_i| - |V_i^{sp}|}{\Delta V_i^{Lim}}\right)^{2n}$$

where:

 $|V_i|$  is the voltage magnitude at bus i

 $|V_i^{sp}|$  is the specified (rated) voltage magnitude at bus i

 $\Delta V_i^{Lim}$  is the voltage deviation limit, above which voltage deviations are unacceptable

n is the exponent of penalty function (n = 1 is preferred)

NB is the number of buses in the system

 $W_{V_i}$  is the real non-negative weighting factor

## I. Index for Voltage Analysis

- Recall:  $\Delta V_i^{Lim}$  is the voltage deviation limit, above which voltage deviations are unacceptable
  - If voltage is outside this limit,  $PI_V$  will be large
  - If voltage is within this limit,  $PI_V$  will be small
- Thus  $PI_V$  allows us to rank contingencies based on severity using the voltage limits on the system buses involved
- Problem: bus voltages depend on reactive power flow, which is not considered in this index
  - What if generators are driven to their reactive power (Q) limits?
- Solution: revised index to include reactive power constraints

## I. Index for Voltage Analysis

$$PI_{VQ} = \sum_{i=1}^{NB} \frac{W_{V_i}}{2n} \left(\frac{|V_i| - |V_i^{Sp}|}{\Delta V_i^{Lim}}\right)^{2n} + \sum_{i=1}^{NG} \frac{W_{Q_i}}{2n} \left(\frac{Q_i}{Q_i^{Max}}\right)^{2n}$$

where:

 $|V_i|$  is the voltage magnitude at bus i

 $|V_i^{sp}|$  is the specified (rated) voltage magnitude at bus i

 $\Delta V_i^{Lim}$  is the voltage deviation limit, above which voltage deviations are unacceptable

n is the exponent of penalty function (n = I is preferred)

NB is the number of buses in the system

 $W_{V_i}$  is the real non-negative weighting factor

 $Q_i$  is the reactive power produced at bus i

 $Q_i^{Max}$  is the reactive power production limit

NG is the number of reactive power production units

 $W_{Q_i}$  is the real non-negative weighting factor (set to 0 if not required)

## 2. Index for Power Flow Analysis

$$PI_{MW} = \sum_{l=1}^{NL} \frac{W_l}{2n} \left(\frac{P_l}{P_l^{Lim}}\right)^{2n}$$

where:

 $P_l$  is the megawatt flow of line *l* (calculated by the DC load flow model)

 $P_l^{Lim}$  is the megawatt capacity of line *l* 

NL is the number of lines in the system

n is the specified exponent (n = I is preferred)

 $W_l$  is the real non-negative weighting coefficient; may be used to reflect importance of some lines

## 2. Index for Power Flow Analysis

• Recall:  $P_l^{Lim}$  is the line capacity limit

- If line flows exceed their limits, Pl<sub>MW</sub> will be large
- If line flows are within their limits,  $PI_{MW}$  will be small
- The absolute value of  $PI_{MW}$  for each outage is not significant
  - Ranking is done by comparing  $\text{PI}_{\text{MW}}$  for each outage and looking at the relative change
  - This is done by looking at the results of the DC load flow solution before the outage (base case) and after the outage (adjoint power system

## Other Contingency Ranking Methods

- I. Distribution factor method
  - Very fast, but not very accurate
  - Can be used to prescreen contingencies for AC load flow
  - Does not provide voltage prediction
- Ranking based on assumption that the loss of a heavily loaded line would likely result in overloads on other lines
  - 2. Ranking in order of most heavily loaded to least
  - 3. Ranking in order of absolute magnitudes of line flows
  - Both methods were considered, but were determined to not provide proper contingency selection

## CREATING ORDERED CONTINGENCY LISTS

## **Contingency List Options**

Option	Performance Index	Outage Type
I. I.	$PI_V$ or $PI_{VQ}$	Line and/or generator outages
2	$PI_{MW}$	Line outages
3	PI <sub>MW</sub>	Generator outages (Allows for redispatch of the lost generation)

 May focus on only one option, or repeat procedure to look at all three

## Tellegen's Theorem

- All three options give sensitivities in terms of incremental change in performance index to an incremental change in line admittance or generator output
  - The full effect would be found my multiplying the derivative by the full line admittance using Tellegen's Theorem
- Tellegen's Theorem: allows rapid computation of gradient vectors which contain the performance index derivatives
- Resulting normalized numbers represent the  $\Delta \text{PI}$  for each contingency
  - Misorderings may occur due to the linear approximation
  - Non-perfect ranking is ok because the stopping criteria will cover that

## NUMERICAL EXAMPLES

- EHV backbone of the ITAIPU transmission system
- Scheme designed for use in Brazil over Ione 800 kV lines



- System has synchronous generators and reactors
- Has had previous indications of reliability issues
- Chosen to be a test case for the voltage performance index  $PI_V$  with line outages only (Option I)
  - $\Delta V_i^{Lim}$  was set to 0.075 pu (±7.5% voltage threshold)

Comparison of AC Load Flow and Contingency Ranking Algorithm for the Voltage Index on 11-Bus System

Line Outage Ranking by AC Load Flow			Line Outage Ranking by Contingency Selector			
Ordered Line Numbers	Voltage Performance Index PI <sub>V</sub>	Worst % of Out-of- Limit Voltage	Ordered Line Numbers	Normalized Sensitivity ( $\Delta$ PI)		
7	1.9697	1.24	7	0.2676		
8	1.4341	0.97	8	0.2475		
9	1.127	0.93	9	0.1784		
5	0.9878	0.78	5	0.1445		
4	0.8073	0.72	6	0.0659		
6	0.6182	0.64	12	0.0364		
12	0.4861	0.67	П	0.0322		
П	0.4797	0.64	10	0.0314		
10	0.4654	0.67	4	0.0236		
3	0.4374	0.60	15	0.0022		
2	0.4310	0.60	13	0.0002		
13	0.4273	0.61	I	-0.2504E-5		
15	0.4271	0.60	2	-0.1295E-4		
14	0.4252	0.60	3	-0.2171E-4		
I	0.4198	0.59	14	-0.2101E-4		

Effectiveness Profile of Voltage Performance Index for 11-Bus System



Comparison of Voltages and Voltage Indices for Worst Three Outages on 11-Bus System

Bus	Base Case Voltages	Line 7 Outage	Line 8 Outage	Line 9 Outage
I	0.9950	0.9950	0.9950	0.9950
2	1.0000	1.0000	1.0000	1.0000
3	0.9807	0.9693	0.9875	0.9810
4	0.9900	0.9346	0.9547	0.9398
5	0.9517	0.9021	0.9938	0.9669
6	0.9469	0.9354	0.9295	0.9380
7	0.9443	0.9199	0.9392	0.9291
8	0.9700	0.9700	0.9655	0.9700
9	0.9657	0.9665	0.9700	0.9700
10	0.9778	0.9782	0.9782	0.9792
П	0.9900	0.9900	0.9900	0.9900
	Voltage Index	1.9697	1.4341	1.1270

## Test System #2 – 29-Bus System

• A modified version of the IEEE 30-bus system as shown below



#### Test System #2 – 29-Bus System

• Chosen as a test case for  $PI_{VQ}$  (Option I) with line outages and  $PI_{MW}$  with line outages (Option 2)



## Test System #3 – 10-Bus CIGRE System

- System has seven generating plants
- Chosen as a test case for  $PI_{VQ}$  (Option I) with generator outages and  $PI_{MW}$  with generator outages (Option 3)

Contingency Selection Rankings on 10-Bus CIGRE System

AC Load Flow		Contingency Selection			DC Lo	oad Flow	Contingency Selection	
Ordered Generator Numbers	Voltage Performance Index PI <sub>V</sub>	Ordered Generator Numbers	Normalized Sensitivity (ΔΡΙ)	Worst Bus Voltage	Ordered Generator Numbers	Voltage Performance Index PI <sub>MW</sub>	Ordered Generator Numbers	Normalized Sensitivity $(\Delta PI_{MW})$
3	0.9543	3	0.4832	0.818	3	1.6932	3	0.4699
5	0.9215	5	0.1849	0.834	7	0.7985	4	0.1683
6	0.6912	6	0.1383	0.886	4	0.6589	6	0.1442
7	0.3136	4	0.1165	0.965	6	0.6157	7	0.1418
4	0.3010	2	0.0065	0.970	5	0.4818	5	0.0386
2	0.1373	7	-0.3059	0.983	I	0.3188	I	-0.3328
L	Swing bus generator excluded from voltage ranking				2	0.1935	2	-0.9597

#### Ranking for Voltage Analysis

#### Ranking for Line Overloads

## STOPPING CRITERIA FOR ADAPTIVE CONTINGENCY PROCESSOR

### Advanced Contingency Processor



## Stopping Criteria

- Simplest option would be to stop as soon as a case showed an out-of-limit condition
  - This would work for some cases, but not others
- A better option is to do the load flows and stop once there were no out-of-limit conditions X times in a row
  - X would be determined by experience
- Another option is to just run N number of cases, regardless of if there are out-of-limit conditions are not
  - N would be determined by experience, but typically between 1 and 20
- One referenced program ran N primary outages and X secondary outages, combining the second two options above

## CONCLUSIONS

## Summary

- Algorithm presented increases the effectiveness of existing contingency analysis techniques
  - Provides an ordered list of contingencies to identify those which are likely to cause the most sever system issues
  - Process creates a list of primary contingencies and then lists for secondary contingencies
  - Will enable system operators to identify weaknesses more quickly
- Ranking algorithm is not perfect, and requires user input for the stopping criteria
- Process has been applied to single outage contingency cases
  - Further work anticipated for multiple outages